

Prediction and Time

Even if we cannot time-travel, perhaps we can do it "virtually"

if we know exactly how a system works & how it changes with time, we should be able to predict its future.

What can we predict?

Deterministic systems: i.e. systems whose future can be predicted exactly e.g. planetary system, mass on a spring, pendulum.

Random systems: i.e. ones which are too complex to predict exactly e.g. gas, society...Best we can do is to predict average values

However there are two other kinds of systems:

<u>Chaotic:</u> i.e. systems which are predictable over the short term but not over the long term.

Quantum: systems which are intrinsically unpredictable except in a special sense.

Chaotic Motion

She comes, she comes, the sable throne behold Of Night Primeval and of Chaos old!

••

Physic of Metaphysic begs defence And Metaphysic calls for aid on Sense See Mystery to Mathematics fly In vain! they gaze, turn giddy, rave and die

Lo! thy Dread Empire, Chaos is restored Light dies before thy uncreating Word. Alexander Pope, The Dunciad

The easiest one to visualize, although technically it is not chaotic, is the "baker transform".

- Take a piece of dough with a raisin
- Stretch it to twice it's original length
- Fold it in half
- Where is the raisin?
- The formula is
 - $x_n = 2x_{n-1} (x_{n-1} < .5)$ $x_n = 2 - 2x_{n-1} (x_{n-1} > .5)$



For example, we can start with two raisins very close together and see what happens: • If you plot the difference in their positions, it looks

nice and smooth to start with, but suddenly becomes random.







• So total number in next generation is

$$x_{n+1} = x_n - x_{death} - x_{starve} + x_{birth}$$
$$= (1 + k - k')x_n - k''x_n^2$$











Logistic Map

• VALENTINE "You have some x-and-y equations. Any value for x gives you a value for y. So you put a dot where it's right for both x and y. Then you take the next value for x which gives you another value for y, and when you've done that a few times you join up the dots and that's your graph of whatever the equation is....every time she works out a value for y, she's using that as her next value of x. And so on." Arcadia

Chaotic Systems

All chaotic systems have some common features

- \bullet The equations must all be non-linear: i.e. Have terms like x^2
- There are regions of the parameters where the motion is predictable
- There are regions where it is chaotic
- In the chaotic region, points that start off close together become wildly different as time goes on.







Weather

- <u>"Primitive Equations"</u> for weather written down by L F Richardson (1922). Can't be solved without computer
- Assume we know everything (temperature, pressure, humidity, radiation inflow...) at some points in space.
- \times
- Each point will affect it's neighbour, so can figure out how it will change
- Need to know how the energy can be transferred

- Note that all these processes work together
- e.g your coffee!



This is how we do it



But

Butterfly effect found in 1950's: arbitrarily small perturbation of initial conditions have unpredictably large consequences.

• The "Lorentz" equations: very simplified version of the "weather " equations, give rise to chaotic behaviour.

Weather is also chaotic

- You cannot predict the future weather precisely.
- However, buried in this are some predictable elements. e.g. we <u>cannot</u> predict an "el Nino" event, but we <u>can</u> predict the consequences once it has happened.
- Note "weather" prediction and "climate" prediction are (almost) unrelated

•Can predict globally, not locally Can predict how fast a river will flow





• But not how it will behave on small scale





Can do it over the short term Hurricane Isabelle



An interesting chaotic system (provided your pension doesn't depend on it!)



others equity. Such tight coupling increases the danger of "non-linear" outcomes, where a small change has a big impact. Economist Feb 2010

Now we do the hard stuff

- Quantum Mechanics
- I think I can safely say that nobody understands quantum mechanics. (Richard Feynman.)

What is light?

Particle? Newton, Descartes

- Kerner: Look at the edge of the shadow. It is straight like the edge of the wall that makes it. This means light is ..little bullets. Bullets go straight. Hapgood (Tom Stoppard)
- Wave? Young, Huyghens
- Kerner: When you shine a light through two little gaps, side by side, you don't get particle patterns like for bullets, you get wave patterns like for water. The two beams of light mix together Hapgood (Tom Stoppard)
- Yes? Planck/Einstein
- Light travels as wave, but arrives and departs as particle

Wave-Particle Duality

De Broglie 1924

- You cannot ask: Is light a wave or a particle: answer is "yes"
- Einstein/Planck suggest light (wave) has some particle properties: "particle" of light is photon (γ : gamma)
- so maybe electron (particle) has some wave properties
- Wave particle duality:
- All fundamental (i.e small!) particles also act like waves (what is an electron?...) and waves act like particles.

Waves in General

• Can show "interference" : sometimes waves will add together, sometimes cancel out







- With the (in principle) simple assumption that waves ⇔ particleswe can also understand
- **Antiparticles:** For every particle with given properties, there is a corresponding anti-particle with the properties flipped:
 - e.g. electron has charge -1.6x10⁻¹⁹ C
 - positron has same mass, charge = 1.6×10^{-19} C
- Solids and liquids: e.g why copper is a good conductor and plastic is a lousy one
- Nuclear forces (why don't they simply fall apart, what makes uranium radio-active, but not lead)
- Transistors and hence integrated circuits
- Light in fibres
- Stars (how long will the sun last, and what will happen to it)
- Superconductors (why some materials conduct electricity perfectly)
- Lasers (another idea that started with Einstein)
- Magnetic Resonance Imaging (MRI)

Since quantum mechanics works so well, maybe we shouldn't worry about what it actually means....

- But we have some problems:
- Which slit did the electron go through?
- We choose to examine a phenomenon which is impossible, absolutely impossible, to explain in any classical way, and which has in it the heart of the quantum mechanics. In reality it contains the only mystery...Any other situation in QM, it turns out, can always be explained by saying, "You remember the case of the experiment with the two holes? It's the same thing."
- Richard Feynman, the Character of Physical Law

What Waves?





- Suppose we get sneaky and allow electron through but check which slit it went through.
- Now we get sum of one slit patterns, but not a 2 slit pattern!
- What happens if we use a detector that only picks up one electron in two?
- More worrying than this: we can do a "delayed choice" experiment: don't try to observe the electron until after it has gone through one of the slits...that still destroys the pattern.
- Conclusion We cannot decide which slit the electron went through without destroying the pattern. Observing something fundamentally changes it!

- There was a young man who said "God Must think it exceedingly odd That this tree Continues to be When there's no one about in the Quad"
- · Kerner: Now we come to the exciting part. We will watch the bullet to see how they make waves ... The wave pattern has disappeared Because we looked. Every time we don't look, we get wave pattern. Every time we look to see how we get wave pattern we get particle pattern Hapgood (Tom Stoppard)

So why should you care, since this is a lecture about Time?

- Because we cannot say what happened **after** it happened!
- I can only say, there we have been: but I cannot say where. And I cannot say, how long, for that is to place it in time. T. S. Eliot (Burnt Norton)



What Waves?





Probability Interpretation

- Wave represents probability of particle being at given place: more precisely
- Note Electron must be somewhere: i.e. probability of detecting it somewhere = 1
- Think of a die:
- probability of any given face = 1/6
- probability of any face being uppermost = 1





Classical Determinism

- Given state of solar system in (say) 100 A. D., can use Newtonian mechanics to predict earth's position now
- Quantum mechanics:
- Can only predict most likely (probable) position now.

• Morals

- 1.Macroscopic (i.e. large) objects are predictable, electrons aren't!
- 2.Cannot ask "what happens?": can only ask "what can we measure?"
- 3.No reason to assume that rules deduced for macroscopic objects are true for very large/very light/ very fast objects.
- 4."What colour is an electron?"

Measurement

- In classical mechanics, we believe that a object is the same whether we measure it or not.
- In quantum mechanics, until we have measured it, its condition is indeterminate.
- E.g.: suppose we measure the position of a particle and it was here →C
- Where was it just before?
- •Classical Mechanic At C.
- •Quantum Mechanic Somewhere: it was only measuring it that fixed its position . Where is a candle flame after it is blown out?

Have we given free will to the electron?

- E.g. go back to our wave function example:
- This seemed to say that the electron gets split in half, but we interpreted it as a probability.
- But when did the electron decide which way it was going?



- Classical Mechanic Obviously at the moment it was reflected.
- Quantum Mechanic It is indeterminate until you measure it
- The Einstein-Podolsky-Rosen paradox (EPR) is a more sophisticated version of this
- God does not play dice. Einstein
- Only way out is "hidden variables": underneath quantum mechanics, there is some "clockwork". it only looks random on the surface.

Schrödinger's Cat

shows the idiocy of people who really believe in quantum mechanics.

- You have a box, with a lid and a single radioactive atom: when the atom decays, cyanide gas is released.
- Take a cat
- Put it in the box and close the lid.
- Is the cat dead or alive?



•Classical Mechanic Obviously its either dead or alive

- Quantum Mechanic It is indeterminate until you measure it . More exactly, the cat is a mixture of alive and dead cats: the measurement fixes it.
- Schrödinger Don't be stupid.

Both Einstein and Schrödinger were wrong.

Bell's theorem shows that there is a measurement that you can do on the polarizations of the particles which is incompatible with any possible hidden variable theory.

- Aspect did the experiment.
- The Schrödinger's Cat experiment has been done:
- No animals were injured in the making of this movie.
- One atom: process is totally random, so you can't decide if a one-atom cat is alive or dead without measuring it(!)
- Many atoms (10²⁹): constitutes an independent measuring system, so the cat measures it's own deadness
- Few atoms (2-20): process becomes steadily more predictable
- God not only plays dice, but throws them where they cannot be seen. *Hawking*

- We can calculate measured values with phenomenal accuracy
- E.g. An electron acts like a tiny magnet: exactly how tiny?
- In sensible units
- -1.001159652181 (2006 measured)
- -1.001159652182 (2008 theory)
- So quantum mechanics cannot be *Wrong*

The quantum Zeno effect

If measuring something really matters, then we can "reset the clock" by making sure that nothing has happened.

Hence watching a cold pot on a stove makes sure it never boils:

in more sophisticated language, if you continuously measure the state of an atom to make see if it hasn't decayed, then it can't!



Measurement

- This "measurement fixes things" is known as the "Collapse of wave function": obviously very ugly .
- How does the electron know it is being measured?.
- Do we need an actual conscious observer?
- Is there a link between consciousness and QM?

Many worlds theory

Everett (1957) . Every time a measurement is made, the universe subdivides into separate universes that correspond to every possible outcome



"You're in the right place and this is the right time, but I'm afraid you're in the wrong alternate universe."

Avoids observation problems, but not testable (?) and not very economical! In all fictional works, each time a man is confronted with several alternatives, he chooses one and eliminates the others; in the fiction of Ts'ui Pên, he choosessimultaneously-- all of them. He creates in the diverse way, diverse futures..which themselves also proliferate and fork.

The Garden of Forking Paths, Borges.

What might have been is an abstraction Remaining a perpetual possibility Only in a world of speculation. What might have been and what has been Point to one end, which is always present. Footfalls echo in the memory Down the passage which we did not take Towards the door we never opened Into the rose-garden. T. S. Eliot (Burnt Norton)

Conclusions:

Either Quantum mechanics is correct, and there is no "simpler" system

- Or Reality is even uglier than we thought: e.g.
- non-local hidden variables: every bit of the universe is involved with every other bit:
- very Zen, but totally wipes out free will!
- (Ugh!)

Conclusions:

Does it bother you that 20th century technology depends fundamentally on something no-one understands?

I can only say, **there** we have been: but I cannot say where. And I cannot say, how long, for that is to place it in time.

T. S. Eliot (Burnt Norton)

Where does this leave prediction?

- Predictions (especially of the future) are hard!
- We can PROVE some very simple systems with exact equations are unpredictable
- We (more-or-less) understand what systems are predictable
- Some very complex systems ARE partly predictable
- Quantum systems allow very accurate average predictions but no individual predictions
- And seem to forbid retrodictions!